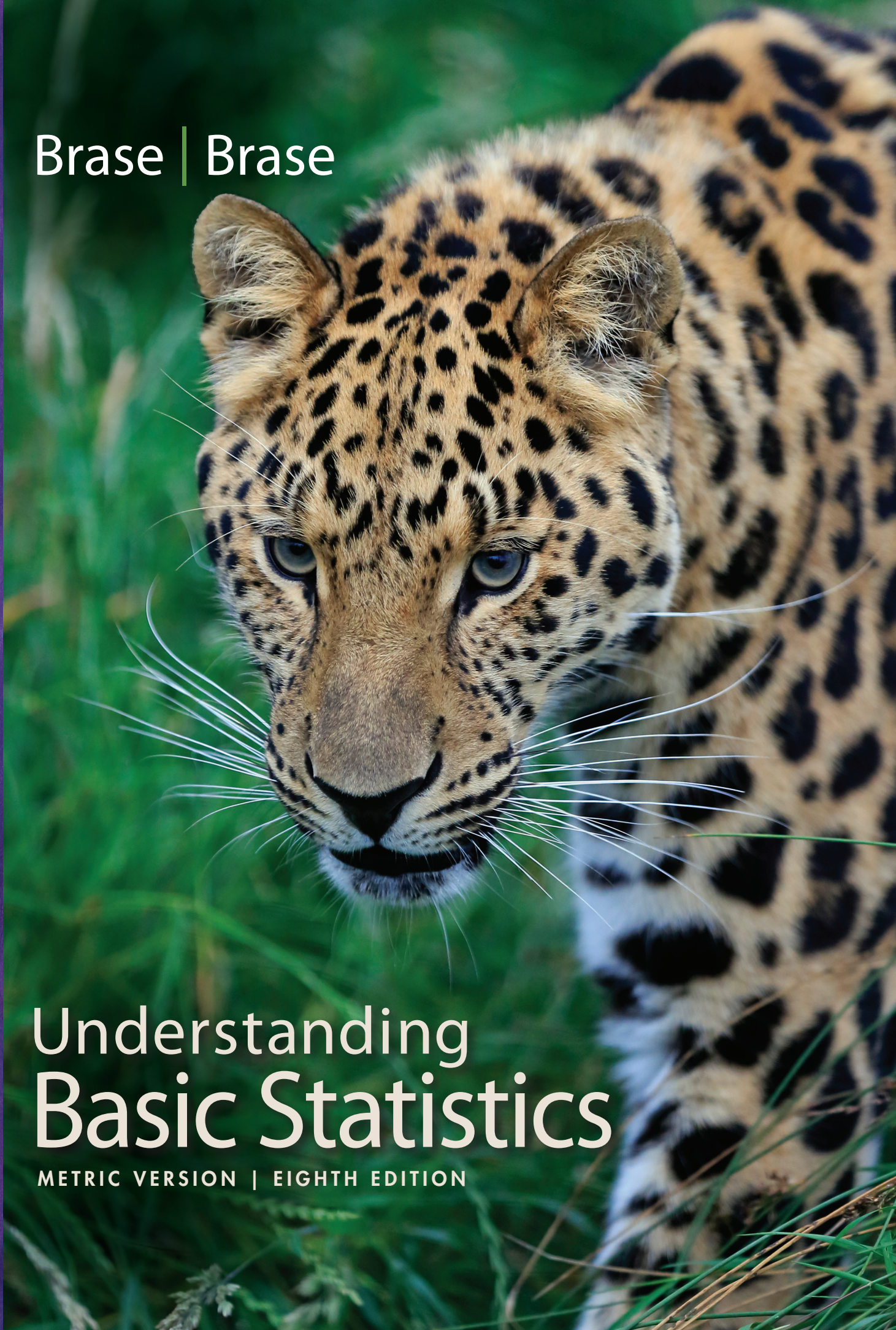


METRIC VERSION

Brase | Brase

Understanding Basic Statistics

METRIC VERSION | EIGHTH EDITION



Understanding Basic Statistics, Eighth Edition, Metric Version

8E

Understanding Basic Statistics, Eighth Edition, Metric Version

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Professor Emeritus, Alexandria University, Egypt



*This book is dedicated to the memory of
a great teacher, mathematician, and friend*
Burton W. Jones
Professor Emeritus, University of Colorado



**Understanding Basic Statistics,
Eighth Edition, Metric Version**

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Index I1

Critical Thinking

Students need to develop critical thinking skills in order to understand and evaluate the limitations of statistical methods. *Understanding Basic Statistics*, Eighth Edition, Metric Version makes students aware of method appropriateness, assumptions, biases, and justifiable conclusions.

CRITICAL THINKING

UNUSUAL VALUES

Chebyshev's theorem tells us that no matter what the data distribution looks like, at least 75% of the data will fall within 2 standard deviations of the mean. As we will see in Chapter 7, when the distribution is mound-shaped and symmetric, about 95% of the data are within 2 standard deviations of the mean. Data values beyond 2 standard deviations from the mean are less common than those closer to the mean.

In fact, one indicator that a data value might be an outlier is that it is more than 2.5 standard deviations from the mean (Source: *Statistics*, by G. Upton and I. Cook, Oxford University Press).

UNUSUAL VALUES

For a binomial distribution, it is unusual for the number of successes r to be higher than $\mu + 2.5\sigma$ or lower than $\mu - 2.5\sigma$.

We can use this indicator to determine whether a specified number of successes out of n trials in a binomial experiment are unusual.

For instance, consider a binomial experiment with 20 trials for which probability of success on a single trial is $p = 0.70$. The expected number of successes is $\mu = 14$, with a standard deviation of $\sigma \approx 2$. A number of successes above 19 or below 9 would be considered unusual. However, such numbers of successes are possible.

◀ Critical Thinking

Critical thinking is an important skill for students to develop in order to avoid reaching misleading conclusions. The Critical Thinking feature provides additional clarification on specific concepts as a safeguard against incorrect evaluation of information.

Interpretation ▶

Increasingly, calculators and computers are used to generate the numeric results of a statistical process. However, the student still needs to correctly interpret those results in the context of a particular application. The Interpretation feature calls attention to this important step. Interpretation is stressed in examples, in guided exercises, and in the problem sets.

SOLUTION: Since we want to know the number of standard deviations from the mean, we want to convert 196 to standard z units.

$$z = \frac{x - \mu}{\sigma} = \frac{196 - 227}{14} = -2.21$$

Interpretation The amount of cheese on the selected pizza is only 2.21 standard deviations below the mean. The fact that z is negative indicates that the amount of cheese is 2.21 standard deviations *below* the mean. The parlor will not lose its franchise based on this sample.

- Interpretation** A campus performance series features plays, music groups, dance troops, and stand-up comedy. The committee responsible for selecting the performance groups include three students chosen at random from a pool of volunteers. This year the 30 volunteers came from a variety of majors. However, the three students for the committee were all music majors. Does this fact indicate there was bias in the selection process and that the selection process was not random? Explain.
- Critical Thinking** Greg took a random sample of size 100 from the population of current season ticket holders to State College men's basketball games. Then he took a random sample of size 100 from the population of current season ticket holders to State College women's basketball games.
 - What sampling technique (stratified, systematic, cluster, multistage, convenience, random) did Greg use to sample from the population of current season ticket holders to all State College basketball games played by either men or women?
 - Is it appropriate to pool the samples and claim to have a random sample of size 200 from the population of current season ticket holders to all State College home basketball games played by either men or women? Explain.

◀ Critical Thinking and Interpretation Exercises

In every section and chapter problem set, Critical Thinking problems provide students with the opportunity to test their understanding of the application of statistical methods and their interpretation of their results. Interpretation problems ask students to apply statistical results to the particular application.

Statistical Literacy

No language, including statistics, can be spoken without learning the vocabulary. *Understanding Basic Statistics*, Eighth Edition, Metric Version introduces statistical terms with deliberate care.

What Does the Level of Measurement Tell Us?

The level of measurement tells us which arithmetic processes are appropriate for the data. This is important because different statistical processes require various kinds of arithmetic. In some instances all we need to do is count the number of data that meet specified criteria. In such cases nominal (and higher) data levels are all appropriate. In other cases we need to order the data, so nominal data would not be suitable. Many other statistical processes require division, so data need to be at the ratio level. Just keep the nature of the data in mind before beginning statistical computations.

What Does (concept, method, statistical result) Tell Us?

This feature gives a brief summary of the information we obtain from the named concept, method, or statistical result.

Important Features of a (concept, method, or result) ►

In statistics we use many different types of graphs, samples, data, and analytical methods. The features of each such tool help us select the most appropriate ones to use and help us interpret the information we receive from applications of the tools.

Important Features of a Simple Random Sample

For a simple random sample

- Every sample of specified size n from the population has an equal chance of being selected.
- No researcher bias occurs in the items selected for the sample.
- A random sample may not always reflect the diversity of the population. For instance, from a population of 10 cats and 10 dogs, a random sample of size 6 could consist of all cats.

SECTION 7.1 PROBLEMS

1. **Statistical Literacy** Which, if any, of the curves in Figure 7-7 look(s) like a normal curve? If a curve is not a normal curve, tell why.
2. **Statistical Literacy** Look at the normal curve in Figure 7-8, and find μ , $\mu + \sigma$, and σ .

FIGURE 7-7

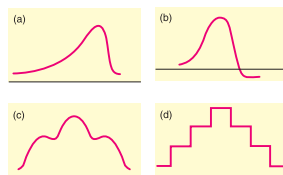
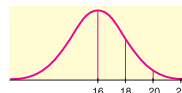


FIGURE 7-8



8. **Terminology** Consider the following statement: If you answered 90% of the questions on a test correctly, then your score is in the 90th percentile. Is the statement true or false? Explain.
9. **Statistical Literacy**
 - (a) What measures of variation indicate spread about the mean?
 - (b) Which graphic display shows the median and the data spread about the median?

Statistical Literacy and NEW Terminology Problems

In every section and chapter problem set, Statistical Literacy problems test student understanding of terminology, statistical methods, and the appropriate conditions for use of the different processes. NEW terminology problems in each chapter problem set provide multiple choice or true/false questions related to terminology.

Definition Boxes ►

Whenever important terms are introduced in text, blue definition boxes appear within the discussions. These boxes make it easy to reference or review terms as they are used further.

Box-and-Whisker Plots

The quartiles together with the low and high data values give us a very useful *five-number summary* of the data and their spread.

FIVE-NUMBER SUMMARY

Lowest value, Q_1 , median, Q_3 , highest value

We will use these five numbers to create a graphic sketch of the data called a *box-and-whisker plot*. Box-and-whisker plots provide another useful technique from exploratory data analysis (EDA) for describing data.

IMPORTANT WORDS & SYMBOLS

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◀ Important Words & Symbols

The Important Words & Symbols within the Chapter Review feature at the end of each chapter summarizes the terms introduced in the Definition Boxes for student review at a glance. Page numbers for first occurrence of term are given for easy reference.

Linking Concepts: Writing Projects ▶

Much of statistical literacy is the ability to communicate concepts effectively. The Linking Concepts: Writing Projects feature at the end of each chapter tests both statistical literacy and critical thinking by asking the student to express their understanding in words.

LINKING CONCEPTS: WRITING PROJECTS

Discuss each of the following topics in class or review the topics on your own. Then write a brief but complete essay in which you summarize the main points. Please include formulas and graphs as appropriate.

1. What does it mean to say that we are going to use a sample to draw an inference about a population? Why is a random sample so important for this process? If we wanted a random sample of students in the cafeteria, why couldn't we just choose the students who order Diet Pepsi with their lunch? Comment on the statement, "A random sample is like a miniature population, whereas samples that are not random are likely to be biased." Why would the students who order Diet Pepsi with lunch not be a random sample of students in the cafeteria?
2. In your own words, explain the differences among the following sampling techniques: simple random sample, stratified sample, systematic sample, cluster sample, multistage sample, and convenience sample. Describe situations in which each type might be useful.

5. **Basic Computation: Central Limit Theorem** Suppose x has a distribution with a mean of 8 and a standard deviation of 16. Random samples of size $n = 64$ are drawn.
 - (a) Describe the \bar{x} distribution and compute the mean and standard deviation of the distribution.
 - (b) Find the z value corresponding to $\bar{x} = 9$.
 - (c) Find $P(\bar{x} > 9)$.
 - (d) **Interpretation** Would it be unusual for a random sample of size 64 from the x distribution to have a sample mean greater than 9? Explain.

◀ Basic Computation Problems

These problems focus student attention on relevant formulas, requirements, and computational procedures. After practicing these skills, students are more confident as they approach real-world applications.

Expand Your Knowledge Problems ▶

Expand Your Knowledge problems present optional enrichment topics that go beyond the material introduced in a section. Vocabulary and concepts needed to solve the problems are included at point-of-use, expanding students' statistical literacy.



30. **Expand Your Knowledge: Geometric Mean** When data consist of percentages, ratios, compounded growth rates, or other rates of change, the *geometric mean* is a useful measure of central tendency. For n data values,

$$\text{Geometric mean} = \sqrt[n]{\text{product of the } n \text{ data values}}, \text{ assuming all data values are positive}$$

To find the *average growth factor* over 5 years of an investment in a mutual fund with growth rates of 10% the first year, 12% the second year, 14.8% the third year, 3.8% the fourth year, and 6% the fifth year, take the geometric mean of 1.10, 1.12, 1.148, 1.038, and 1.16. Find the average growth factor of this investment.

Direction and Purpose

Real knowledge is delivered through direction, not just facts. *Understanding Basic Statistics*, Eighth Edition, Metric Version ensures the student knows what is being covered and why at every step along the way to statistical literacy.

Chapter Preview Questions

Preview Questions at the beginning of each chapter give the student a taste of what types of questions can be answered with an understanding of the knowledge to come.

Normal Curves and Sampling Distributions

PREVIEW QUESTIONS

PART I

What are some characteristics of a normal distribution? What does the empirical rule tell you about data spread around the mean? How can this information be used in quality control? (SECTION 7.1)

Can you compare apples and oranges, or maybe elephants and butterflies? In most cases, the answer is no—unless you first standardize your measurements. What are a standard normal distribution and a standard z score? (SECTION 7.2)

How do you convert any normal distribution to a standard normal distribution? How do you find probabilities of “standardized events”? (SECTION 7.3)



Photo credit: Shutterstock.com

FOCUS PROBLEM

Benford's Law: The Importance of Being Number 1

Benford's Law states that in a wide variety of circumstances, numbers have “1” as their first nonzero digit disproportionately often. Benford's Law applies to such diverse topics as the drainage areas of rivers; properties of chemicals; populations of towns; figures in newspapers, magazines, and government reports; and the half-lives of radioactive atoms!

Specifically, such diverse measurements begin with “1” about 30% of the time, with “2” about 18% of the time, and with “3” about 12.5% of the time. Larger digits occur less often. For example, less than 5% of the numbers in circumstances such as these begin with the digit 9. This is in dramatic contrast to a random sampling situation, in which each of the digits 1 through 9 has an equal chance of appearing.



Photo credit: BRENDAN SMIALOWSKI/AFP/Getty Images

Chapter Focus Problems

The Preview Questions in each chapter are followed by a Focus Problem, which serves as a more specific example of what questions the student will soon be able to answer. The Focus Problems are set within appropriate applications and are incorporated into the end-of-section exercises, giving students the opportunity to test their understanding.

8. **Focus Problem: Benford's Law** Again, suppose you are the auditor for a very large corporation. The revenue file contains millions of numbers in a large computer data bank (see Problem 7). You draw a random sample of $n = 228$ numbers from this file and $r = 92$ have a first nonzero digit of 1. Let p represent the population proportion of all numbers in the computer file that have a leading digit of 1.
- Test the claim that p is more than 0.301. Use $\alpha = 0.01$.
 - If p is in fact larger than 0.301, it would seem there are too many numbers in the file with leading 1s. Could this indicate that the books have been “cooked” by artificially lowering numbers in the file? Comment from the point of view of the Internal Revenue Service. Comment from the perspective of the Federal Bureau of Investigation as it looks for “profit skimming” by unscrupulous employees.
 - Comment on the following statement: “If we reject the null hypothesis at level of significance α , we have not *proved* H_0 to be false. We can say that the probability is α that we made a mistake in rejecting H_0 .” Based on the outcome of the test, would you recommend further investigation before accusing the company of fraud?

Focus Points ►

Each section opens with bulleted Focus Points describing the primary learning objectives of the section.

SECTION 3.1

Measures of Central Tendency: Mode, Median, and Mean

FOCUS POINTS

- Compute mean, median, and mode from raw data.
- Interpret what mean, median, and mode tell you.
- Explain how mean, median, and mode can be affected by extreme data values.
- What is a trimmed mean? How do you compute it?
- Compute a weighted average.

The average price of a gram of gold is \$41. The Zippy car averages 17 kilometers per liter on the highway. A survey showed the average shoe size for women is size 40.

In each of the preceding statements, *one* number is used to describe the entire sample or population. Such a number is called an *average*. There are many ways to compute averages, but we will study only three of the major ones.

The easiest average to compute is the *mode*.

The **mode** of a data set is the value that occurs most frequently. *Note:* If a data set has no single value that occurs more frequently than any other, then that data set has no mode.

EXAMPLE 1

Mode

Count the letters in each word of this sentence and give the mode. The numbers of letters in the words of the sentence are

5 3 7 2 4 4 2 4 8 3 4 3 4

LOOKING FORWARD

In later chapters we will use information based on a sample and sample statistics to estimate population parameters (Chapter 8) or make decisions about the value of population parameters (Chapters 9 and 10).

◀ Looking Forward

This feature shows students where the presented material will be used later. It helps motivate students to pay a little extra attention to key topics.

CHAPTER REVIEW

SUMMARY

In this chapter, you've seen that statistics is the study of how to collect, organize, analyze, and interpret numerical information from populations or samples. This chapter discussed some of the features of data and ways to collect data. In particular, the chapter discussed

- Individuals or subjects of a study and the variables associated with those individuals
- Data classification as qualitative or quantitative, and levels of measurement of data
- Sample and population data. Summary measurements from sample data are called statistics, and those from populations are called parameters.

- Sampling strategies, including simple random, stratified, systematic, multistage, and convenience. Inferential techniques presented in this text are based on simple random samples.
- Methods of obtaining data: Use of a census, simulation, observational studies, experiments, and surveys
- Concerns: Undercoverage of a population, nonresponse, bias in data from surveys and other factors, effects of confounding or lurking variables on other variables, generalization of study results beyond the population of the study, and study sponsorship

▲ Chapter Summaries

The Summary within each Chapter Review feature now also appears in bulleted form, so students can see what they need to know at a glance.

Ethics and Real-World Skills

Statistics is not done in a vacuum. *Understanding Basic Statistics*, Eighth Edition, Metric Version gives students valuable skills for the real world with ethical considerations, technology instruction, genuine applications, actual data, and group projects.

Discussion of Ethics in Statistics

There are many essential ethical considerations in the practice of sampling and research based on statistics. The American Statistical Association has published ethical guidelines that are discussed in this textbook.

ETHICAL PRACTICE IN STATISTICS REQUIRES

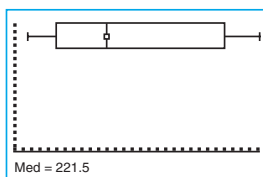
- Transparent and openly stated assumptions regarding data collection and statistical methods used
- Advancement of useful knowledge while avoiding harm to others, especially subjects under study

Tech Notes

Box-and-Whisker Plot

Both Minitab and the TI-84Plus/TI-83Plus/TI-*nspire* calculators support box-and-whisker plots. On the TI-84Plus/TI-83Plus/TI-*nspire*, the quartiles Q_1 and Q_3 are calculated as we calculate them in this text. In Minitab and Excel 2013, they are calculated using a slightly different process.

TI-84Plus/TI-83Plus/TI-*nspire* (with TI-84Plus Keypad) Press **STATPLOT** ► **On**. Highlight box plot. Use **Trace** and the arrow keys to display the values of the five-number summary. The display shows the plot for calories in ice cream bars.



Excel 2013 Does not produce box-and-whisker plot. However, each value of the five-number summary can be found. On the **Home** ribbon, click the **Insert Function** f_x . In the dialogue box, select **Statistical** as the category and scroll to **Quartile**. In the dialogue box, enter the data location and then enter the number of the value you want. For instance, enter 1 in the quartile box for the first quartile.

Minitab Press **Graph** ► **Boxplot**. In the dialogue box, set Data View to **IQRange Box**.

MinitabExpress Press **Graph** ► **Boxplot** ► **simple**.

REVISED! Tech Notes

Tech Notes appearing throughout the text give students helpful hints on using TI-84Plus and TI-*nspire* (with TI-84Plus keypad) and TI-83Plus calculators, Microsoft Excel 2013, Minitab, and Minitab Express to solve a problem. They include display screens to help students visualize and better understand the solution.

REVISED! Using Technology

Further technology instruction is available at the end of each chapter in the Using Technology section. Problems are presented with real-world data from a variety of disciplines that can be solved by using TI-84Plus and TI-*nspire* (with TI-84Plus keypad) and TI-83Plus calculators, Microsoft Excel 2013, Minitab, and Minitab Express.

USING TECHNOLOGY

Binomial Distributions

Although tables of binomial probabilities can be found in most libraries, such tables are often inadequate. Either the value of p (the probability of success on a trial) you are looking for is not in the table, or the value of n (the number of trials) you are looking for is too large for the table. In Chapter 7, we will study the normal approximation to the binomial. This approximation is a great help in many practical applications. Even so, we sometimes use the formula for the binomial probability distribution on a computer or graphing calculator to compute the probability we want.

Applications

The following percentages were obtained over many years of observation by the U.S. Weather Bureau. All data listed are for the month of December.

Location	Long-Term Mean % of Clear Days in Dec.
Juneau, Alaska	18%
Seattle, Washington	24%
Hilo, Hawaii	36%

You may find that using cumulative probabilities and appropriate subtraction of probabilities, rather than addition of probabilities, will make finding the solutions to Applications 3 to 7 easier.

3. Estimate the probability that Juneau will have at most 7 clear days in December.
4. Estimate the probability that Seattle will have from 5 to 10 (including 5 and 10) clear days in December.
5. Estimate the probability that Hilo will have at least 12 clear days in December.
6. Estimate the probability that Phoenix will have 20 or more clear days in December.
7. Estimate the probability that Las Vegas will have from 20 to 25 (including 20 and 25) clear days in December.

Technology Hints

TI-84Plus/TI-83Plus/TI-*nspire* (with TI-84 Plus keypad), Excel 2013, Minitab/MinitabExpress
The Tech Note in Section 6.2 gives specific instructions for binomial distribution functions on the TI-84Plus/

EXAMPLE 11

Central Limit Theorem

A certain strain of bacteria occurs in all raw milk. Let x be the bacteria count per milliliter of milk. The health department has found that if the milk is not contaminated, then x has a distribution that is more or less mound-shaped and symmetric. The mean of the x distribution is $\mu = 2500$, and the standard deviation is $\sigma = 300$. In a large commercial dairy, the health inspector takes 42 random samples of the milk produced each day. At the end of the day, the bacteria count in each of the 42 samples is averaged to obtain the sample mean bacteria count \bar{x} .

(a) Assuming the milk is not contaminated, what is the distribution of \bar{x} ?

SOLUTION: The sample size is $n = 42$. Since this value exceeds 30, the central limit theorem applies, and we know that \bar{x} will be approximately normal, with mean and standard deviation

UPDATED! Applications

Real-world applications are used from the beginning to introduce each statistical process. Rather than just crunching numbers, students come to appreciate the value of statistics through relevant examples.

Most exercises in each section are applications problems. ▶

8. **Ranching: Cattle** You are the foreman of the Bar-S cattle ranch in Colorado. A neighboring ranch has calves for sale, and you are going to buy some to add to the Bar-S herd. How much should a healthy calf weigh? Let x be the age of the calf (in weeks), and let y be the weight of the calf (in kilograms). The following information is based on data taken from *The Merck Veterinary Manual* (a reference used by many ranchers).

x	1	3	10	16	26	36
y	42	50	75	100	150	200

Complete parts (a) through (e), given $\Sigma x = 92$, $\Sigma y = 617$, $\Sigma x^2 = 2338$, $\Sigma y^2 = 82,389$, $\Sigma xy = 13,642$, and $r \approx 0.998$.

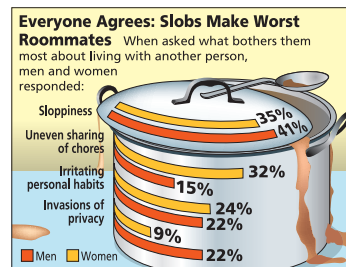
(f) The calves you want to buy are 12 weeks old. What does the least-squares line predict for a healthy weight?

DATA HIGHLIGHTS: GROUP PROJECTS

Break into small groups and discuss the following topics. Organize a brief outline in which you summarize the main points of your group discussion.

1. Examine Figure 2-20, "Everyone Agrees: Slobs Make Worst Roommates." This is a clustered bar graph because two percentages are given for each response category: responses from men and responses from women. Comment about how the artistic rendition has slightly changed the format of a bar graph. Do the bars seem to have lengths that accurately reflect the relative percentages of the responses? In your own opinion, does the artistic rendition enhance or confuse the information? Explain. Which characteristic of "worst roommates" does the graphic seem to illustrate? Can this graph be considered a Pareto chart for men? for women? Why or why not? From the information given in the figure, do you think the survey just listed the four given annoying characteristics? Do you think a respondent could choose more than one characteristic? Explain

FIGURE 2-20



Source: Advantage Business Research for Mattel *Compatibility*

Data Highlights: Group Projects

Using Group Projects, students gain experience working with others by discussing a topic, analyzing data, and collaborating to formulate their response to the questions posed in the exercise.

Making the Jump

Get to the “Aha!” moment faster. *Understanding Basic Statistics*, Eighth Edition, Metric Version provides the push students need to get there through guidance and example.

PROCEDURE

How to test μ when σ is known

Requirements

Let x be a random variable appropriate to your application. Obtain a simple random sample (of size n) of x values from which you compute the sample mean \bar{x} . The value of σ is already known (perhaps from a previous study). If you can assume that x has a normal distribution, then any sample size n will work. If you cannot assume this, then use a sample size $n \geq 30$.

Procedure

1. In the context of the application, state the *null and alternate hypotheses* and set the *level of significance* α .
2. Use the known σ , the sample size n , the value of \bar{x} from the sample, and μ from the null hypothesis to compute the standardized *sample test statistic*.

$$z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}}$$

3. Use the standard normal distribution, two-tailed, to find the *P-value*.
4. *Conclude* the test. If *P-value* then do not reject H_0 .
5. *Interpret your conclusion*.

◀ Procedures and Requirements

Procedure display boxes summarize simple step-by-step strategies for carrying out statistical procedures and methods as they are introduced. Requirements for using the procedures are also stated. Students can refer back to these boxes as they practice using the procedures.

GUIDED EXERCISE 10

Probability Regarding \bar{x}

In mountain country, major highways sometimes use tunnels instead of long, winding roads over high passes. However, too many vehicles in a tunnel at the same time can cause a hazardous situation. Traffic engineers are studying a long tunnel in Colorado. If x represents the time for a vehicle to go through the tunnel, it is known that the x distribution has mean $\mu = 12.1$ minutes and standard deviation $\sigma = 3.8$ minutes under ordinary traffic conditions. From a histogram of x values, it was found that the x distribution is mound-shaped with some symmetry about the mean.

Engineers have calculated that, *on average*, vehicles should spend from 11 to 13 minutes in the tunnel. If the time is less than 11 minutes, traffic is moving too fast for safe travel in the tunnel. If the time is more than 13 minutes, there is a problem of bad air quality (too much carbon monoxide and other pollutants).

Under ordinary conditions, there are about 50 vehicles in the tunnel at one time. What is the probability that the mean time for 50 vehicles in the tunnel will be from 11 to 13 minutes?

We will answer this question in steps.

- (a) Let \bar{x} represent the sample mean based on samples of size 50. Describe the \bar{x} distribution.

➔ From the central limit theorem, we expect the \bar{x} distribution to be approximately normal, with mean and standard deviation

$$\mu_{\bar{x}} = \mu = 12.1 \quad \sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} = \frac{3.8}{\sqrt{50}} \approx 0.54$$

- (b) Find $P(11 < \bar{x} < 13)$.

➔ We convert the interval

$$11 < \bar{x} < 13$$

to a standard z interval and use the standard normal probability table to find our answer. Since

$$z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}} \approx \frac{\bar{x} - 12.1}{0.54}$$

$$\bar{x} = 11 \text{ converts to } z \approx \frac{11 - 12.1}{0.54} = -2.04$$

$$\text{and } \bar{x} = 13 \text{ converts to } z \approx \frac{13 - 12.1}{0.54} = 1.67$$

Therefore,

$$\begin{aligned} P(11 < \bar{x} < 13) &= P(-2.04 < z < 1.67) \\ &= 0.9525 - 0.0207 \\ &= 0.9318 \end{aligned}$$

- (c) **Interpret** your answer to part (b).

➔ It seems that about 93% of the time, there should be no safety hazard for average traffic flow.



Guided Exercises ▶

Students gain experience with new procedures and methods through Guided Exercises. Beside each problem in a Guided Exercise, a completely worked-out solution appears for immediate reinforcement.

Preface

Welcome to the exciting world of statistics! We have written this text to make statistics accessible to everyone, including those with a limited mathematics background. Statistics affects all aspects of our lives. Whether we are testing new medical devices or determining what will entertain us, applications of statistics are so numerous that, in a sense, we are limited only by our own imagination in discovering new uses for statistics.

Overview

The eighth edition of *Understanding Basic Statistics*, Eighth Edition, Metric Version continues to emphasize *concepts of statistics*. Statistical methods are carefully presented with a focus on understanding both the *suitability of the method* and the *meaning of the result*. Statistical methods and measurements are developed in the context of applications.

Critical thinking and interpretation are essential in understanding and evaluating information. Statistical literacy is fundamental for applying and comprehending statistical results. In this edition we have expanded and highlighted the treatment of statistical literacy, critical thinking, and interpretation.

We have retained and expanded features that made the first seven editions of the text very readable. Definition boxes highlight important terms. Procedure displays summarize steps for analyzing data. Examples, exercises, and problems touch on applications appropriate to a broad range of interests.

The eighth edition continues to have extensive online support. Instructional videos are available on DVD. The companion web site at <http://www.cengage.com/statistics/brase8e> contains more than 100 data sets (in JMP, Microsoft Excel, Minitab, SPSS, and TI-84Plus/TI-83Plus/TI-*n*spire with TI-84Plus keypad ASCII file formats) and technology guides.

Major Changes in the Eighth Edition

With each new edition, the authors reevaluate the scope, appropriateness, and effectiveness of the text's presentation and reflect on extensive user feedback. Revisions have been made throughout the text to clarify explanations of important concepts and to update problems.

Current Issues in Statistics Addressed

Brief discussions of ethics in statistics (Section 1.3) and the appropriate use of *P*-values (Section 9.3) as recommended by the American Statistical Association are included. Also included is a brief presentation about data science and big data (Using Technology, Chapter 2).

New Terminology Problems

These problems are included in the chapter problems. They are primarily true/false or multiple choice, highlighting main features of terms or concepts.

Additional Flexibility Provided by Dividing Longer Chapters into Parts

The chapter on Normal Curves and Sampling Distributions (Chapter 7) has been divided into two parts that give appropriate places to pause, review, and summarize content. Each part has a brief introduction, a brief summary, and a list of chapter problems applicable to the part. The same features were added to the last chapter, which includes applications of the chi-square distribution in Part I and inferences for linear regression in Part II.

Revised Examples and New Section Problems

Examples, guided exercises, and problem sets have been updated and revised as necessary.

Updates in Technology Including Minitab Express

Instructions for Excel 2013, Minitab 17, and new Minitab Express are included in the *Tech Notes* and *Using Technology*.

JMP Statistical Software



All new copies of the text now come with JMP statistical software at no additional cost. We realize the vital importance of having a data analysis tool and understand the desirability for students to acquire familiarity with a commercial software package whose use might continue outside of this course. The text can still be used with many other popular software packages as well. See Instructor Resources on page xxvi for a full description of the software.



WebAssign from Cengage

Understanding Basic Statistics, Eighth Edition, Metric Version is a fully customizable online solution for STEM disciplines that empowers you to help your students learn, not just do homework. Insightful tools save you time and highlight exactly where your students are struggling. Decide when and what type of help students can access while working on assignments—and incentivize independent work so help features aren't abused. Meanwhile, your students get an engaging experience, instant feedback and better outcomes. A total win-win!

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Continuing Content

Critical Thinking, Interpretation, and Statistical Literacy

The eighth edition of this text continues and expands the emphasis on critical thinking, interpretation, and statistical literacy. Calculators and computers are very good at providing numerical results of statistical processes. However, numbers from a computer or calculator display are meaningless unless the user knows how to interpret the results and if the statistical process is appropriate. This text helps students determine whether or not a statistical method or process is appropriate. It helps students understand what a statistic measures. It helps students interpret the results of a confidence interval, a hypothesis test, or a linear regression model.

Introduction of Hypothesis Testing Using P -Values

In keeping with the use of computer technology and standard practice in research, hypothesis testing is introduced using P -values. The critical region method is still supported but not given primary emphasis.

Use of Student's t Distribution in Confidence Intervals and Testing of Means

If the normal distribution is used in confidence intervals and testing of means, then the *population standard deviation must be known*. If the population standard deviation is not known, then under conditions described in the text, the Student's t distribution is used. This is the most commonly used procedure in statistical research. It is also used in statistical software packages such as JMP, Microsoft Excel 2013, Minitab, Minitab Express, SPSS, and TI-84Plus/TI-83Plus/TI-*n*spire calculators.

Confidence Intervals and Hypothesis Tests of Difference of Means

If the normal distribution is used, then both population standard deviations must be known. When this is not the case, the Student's t distribution incorporates an approximation for t , with a commonly used conservative choice for the degrees of freedom. Satterthwaite's approximation for the degrees of freedom as used in computer software is also discussed. The pooled standard deviation is presented for appropriate applications ($\sigma_1 \approx \sigma_2$).

Features in the Eighth Edition

Chapter and Section Lead-ins

- *Preview Questions* at the beginning of each chapter are keyed to the sections.
- *Focus Problems* at the beginning of each chapter demonstrate types of questions students can answer once they master the concepts and skills presented in the chapter.
- *Focus Points* at the beginning of each section describe the primary learning objectives of the section.

Carefully Developed Pedagogy

- *Examples* show students how to select and use appropriate procedures.
- *Guided Exercises* within the sections give students an opportunity to work with a new concept. Completely worked-out solutions appear beside each exercise to give immediate reinforcement.
- *Definition boxes* highlight important definitions throughout the text.
- *Procedure displays* summarize key strategies for carrying out statistical procedures and methods. Conditions required for using the procedure are also stated.
- *What Does a concept, method, or result Tell Us?* summarize information we obtain from the named concepts and statistical processes and gives insight for additional application.
- *Important Features of a concept, method, or result* summarize the features of the listed item.
- NEW! Recommendations from the Statistical Association of America regarding the importance of ethics in statistics and appropriate use of P -values are discussed.

- *Looking Forward* features give a brief preview of how a current topic is used later.
- *Labels* for each example or guided exercise highlight the technique, concept, or process illustrated by the example or guided exercise. In addition, labels for section and chapter problems describe the field of application and show the wide variety of subjects in which statistics is used.
- *Section and chapter problems* require the student to use all the new concepts mastered in the section or chapter. Problem sets include a variety of real-world applications with data or settings from identifiable sources. Key steps and solutions to odd-numbered problems appear at the end of the book.
- *Basic Computation problems* ask students to practice using formulas and statistical methods on very small data sets. Such practice helps students understand what a statistic measures.
- *Statistical Literacy problems* ask students to focus on correct terminology and processes of appropriate statistical methods. Such problems occur in every section and chapter problem set.
- *Interpretation problems* ask students to explain the meaning of the statistical results in the context of the application.
- *Critical Thinking problems* ask students to analyze and comment on various issues that arise in the application of statistical methods and in the interpretation of results. These problems occur in every section and chapter problem set.
- *Expand Your Knowledge problems* present enrichment topics such as dotplots, grouped data, estimation of standard deviation from a range of data values, residual plots, relationship between confidence intervals and two-tailed hypothesis tests, and more.
- NEW! *Terminology Problems* at the end of each chapter are true/false or multiple choice questions regarding important features or terms or concepts.
- *Cumulative review problem sets* occur after every third chapter and include key topics from previous chapters. Answers to *all* cumulative review problems are given at the end of the book.
- *Data Highlights and Linking Concepts* provide group projects and writing projects.
- *Viewpoints* are brief essays presenting diverse situations in which statistics is used.
- *Design and photos* are appealing and enhance readability.



Expand Your Knowledge Problems and Quick Overview Topics with Additional Applications

Expand Your Knowledge problems do just that! These are optional but contain very useful information taken from the vast literature of statistics. These topics are not included in the main text but are easily learned using material from the section or previous sections. Although these topics are optional, the authors feel that they add depth and enrich a student's learning experience. Each topic was chosen for its relatively straightforward presentation and useful applications. All such problems and their applications are flagged with a sun logo.

Expand Your Knowledge problems in the eighth edition provide additional topics found in Advanced Placement courses. These topics include logarithmic transformation problems featuring exponential growth and power law applications, linear functions of random variables, and confidence intervals for the slope of the least-squares line. Also new are problems involving stratified sampling and the best estimate for the population mean μ .

Some of the other topics in *Expand Your Knowledge problems* or quick overviews include graphs such as dotplots, donut graphs, and variations on stem-and-leaf plots; outliers in stem-and-leaf plots; harmonic and geometric means; moving averages; calculating odds in favor and odds against; continuous uniform distribution, quick estimate of the standard deviation using the Empirical rule; plus four confidence intervals for proportions; Satterthwaite's approximation for degrees of freedom in confidence intervals and hypothesis tests; relationship between confidence intervals and two-tailed hypothesis testing; pooled

two-sample procedures for confidence intervals and hypothesis tests; resampling (also known as bootstrap); simulations of confidence intervals and hypothesis tests using different samples of the same size; and serial correlation (also called autocorrelation).

For location of these optional topics in the text, please see the index.

Technology Within the Text

- *Tech Notes* within sections provide brief point-of-use instructions for the TI-84Plus, TI-83Plus, and TI-*n*spire (with 84Plus keypad) calculators, Microsoft Excel 2013, Minitab and Minitab Express.
- *Using Technology* sections show the use of SPSS as well as the TI-84Plus, TI-83Plus, and TI-*n*spire (with TI-84Plus keypad) calculators, Microsoft Excel 2013, Minitab 17 and Minitab Express.

Most Recent Operating System for the TI-84Plus/TI-83Plus Calculators

The latest operating system (v2.55MP) for the TI-84Plus/TI-83Plus calculators is also discussed, with new functions such as the inverse t distribution and the chi-square goodness-of-fit test described. One convenient feature of the operating system is that it provides on-screen prompts for inputs required for many probability and statistical functions. This operating system is already on new TI-84Plus/TI-83Plus calculators and is available for download to older calculators at the Texas Instruments web site.

Alternate Routes Through the Text

Understanding Basic Statistics, Eighth Edition, Metric Version is designed to be flexible. It offers the professor a choice of teaching possibilities. In most one-semester courses, it is not practical to cover all the material in depth. However, depending on the emphasis of the course, the professor may choose to cover various topics. For help in topic selection, refer to the Table of Prerequisite Material on page 1.

- *Linear regression*. Chapter 4, Correlation and Regression, may be delayed until after Chapter 9. The descriptive topics of linear regression may then be followed immediately by the inferential topics of linear regression presented in Chapter 11.
- *Probability*. For courses requiring minimal probability, Section 5.1 (What Is Probability?) and the first part of Section 5.2 (Some Probability Rules—Compound Events) will be sufficient.

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Corrinne Pellillo Brase

Additional Resources—Get More from Your Textbook!



JMP is a statistics software for Windows and Macintosh computers from SAS, the market leader in analytics software and services for industry. JMP Student Edition is a streamlined, easy-to-use version that provides all the statistical analysis and graphics covered in this textbook. Once data are imported, students will find that most procedures require just two or three mouse clicks. JMP can import data from a variety of formats, including Excel and other statistical packages, and you can easily copy and paste graphs and output into documents.

JMP also provides an interface to explore data visually and interactively, which will help your students develop a healthy relationship with their data, work more efficiently with data, and tackle difficult statistical problems more easily. Because its output provides both statistics and graphs together, the student will better see and understand the application of concepts covered in this book as well. JMP Student Edition also contains some unique platforms for student projects, such as mapping and scripting. JMP functions in the same way on both Windows and Macintosh platforms and instructions contained with this book apply to both platforms.

Access to this software is available with new copies of the book. Students can purchase JMP standalone via CengageBrain.com or www.jmp.com/getse.



WebAssign from Cengage

Understanding Basic Statistics, Eighth Edition, Metric Version is a fully customizable online solution for STEM disciplines that empowers you to help your students learn, not just do homework. Insightful tools save you time and highlight exactly where your students are struggling. Decide when and what type of help students can access while working on assignments—and incentivize independent work so help features aren't abused. Meanwhile, your students get an engaging experience, instant feedback and better outcomes. A total win-win!

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Instructor Resources

Complete Solutions Manual This manual contains solutions to all exercises from the text, including Chapter Review Exercises, and Cumulative Review Exercises. This manual can be found on the Instructors Companion Site.

Cengage Learning Testing Powered by Cognero A flexible, online system that allows you to

- author, edit, and manage test bank content from multiple Cengage Learning solutions.
- create multiple test versions in an instant.
- deliver tests from your LMS, your classroom or wherever you want.

Companion Web site The companion web site at <http://www.cengage.com/brase> contains a variety of resources:

- Microsoft® PowerPoint® lecture slides
- More than 100 data sets in a variety of formats, including
 - JMP
 - Microsoft Excel 2013
 - Minitab
 - SPSS
 - TI-84Plus/TI-83Plus/TI-nspire with 84plus keypad ASCII file formats
- Technology guides for the following programs
 - JMP
 - TI-84Plus, TI-83Plus, and TI-nspire graphing calculators
 - Minitab software (version 14)
 - Microsoft Excel (2010/2007)
 - SPSS Statistics software

Student Resources

Student Solutions Manual Provides solutions to the odd-numbered section and chapter exercises and to all the Cumulative Review exercises in the student textbook.

Minitab® and IBM SPSS These statistical software packages manipulate and interpret data to produce textual, graphical, and tabular results. Minitab® and/or SPSS may be packaged with the textbook. Student versions are available.

The companion web site at <http://www.cengage.com/statistics/brase8e> contains useful assets for students:

- **Technology Guides** Separate guides exist with information and examples for various technology tools. Guides are available for JMP; the TI-84Plus, TI-83Plus, and TI-*n*spire graphing calculators; Minitab software (version 14); Microsoft Excel (2010/2007); and SPSS Statistics software.
- **Interactive Teaching and Learning Tools** include glossary flashcards, online data sets (in JMP, Microsoft Excel 2013, Minitab, SPSS, and TI-84Plus/TI-83Plus/TI-*n*spire with TI-84Plus keypad ASCII file formats), statistical tables and formulas, and more.

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CengageBrain.com Provides the freedom to purchase online homework and other materials à la carte—exactly what you need, when you need it.

For more information, visit <http://www.cengage.com/statistics/brase8e> or contact your local Cengage Learning sales representative.

Table of Prerequisite Material

Chapter	Prerequisite Sections
1 Getting Started	None
2 Organizing Data	1.1, 1.2
3 Averages and Variation	1.1, 1.2, 2.1
4 Correlation and Regression	1.1, 1.2, 3.1, 3.2
5 Elementary Probability Theory	1.1, 1.2, 2.1
6 The Binomial Probability Distribution and Related Topics	1.1, 1.2, 2.1, 3.1, 3.2, 5.1, 5.2 5.3 useful but not essential
7 Normal Curves and Sampling Distributions (omit 7.6) (include 7.6)	1.1, 1.2, 2.1, 3.1, 3.2, 5.1, 5.2, 6.1 also 6.2, 6.3
8 Estimation (omit 8.3) (include 8.3)	1.1, 1.2, 2.1, 3.1, 3.2, 5.1, 5.2, 6.1, 7.1, 7.2, 7.3, 7.4, 7.5 also 6.2, 6.3, 7.6
9 Hypothesis Testing (omit 9.3) (include 9.3)	1.1, 1.2, 2.1, 3.1, 3.2, 5.1, 5.2, 6.1, 7.1, 7.2, 7.3, 7.4, 7.5 also 6.2, 6.3, 7.6
10 Inferences about Differences (omit 10.3) (include 10.3)	1.1, 1.2, 2.1, 3.1, 3.2, 5.1, 5.2, 6.1, 7.1, 7.2, 7.3, 7.4, 7.5, 8.1, 8.2, 9.1, 9.2 also 6.2, 6.3, 7.6, 9.3
11 Additional Topics Using Inference Part I Chi-Square Applications: 11.1, 11.2, 11.3 (Part II Inferences for Linear Regression: 11.4)	1.1, 1.2, 2.1, 3.1, 3.2, 5.1, 5.2, 6.1, 7.1, 7.2, 7.3, 7.4, 7.5, 9.1 Chapter 4, 8.1, 8.2, 9.1, 9.2 also

1

- 1.1 What Is Statistics?
- 1.2 Random Samples
- 1.3 Introduction to Experimental Design



Paul Spinelli/Major League Baseball/Getty Images



Bettmann/Historical/Corbis

Chance favors the prepared mind.

—LOUIS PASTEUR

Statistical techniques are tools of thought . . . not substitutes for thought.

—ABRAHAM KAPLAN

Louis Pasteur (1822–1895) is the founder of modern bacteriology. At age 57, Pasteur was studying cholera. He accidentally left some bacillus culture unattended in his laboratory during the summer. In the fall, he injected laboratory animals with this bacilli. To his surprise, the animals did not die—in fact, they thrived and were resistant to cholera.

When the final results were examined, it is said that Pasteur remained silent for a minute and then exclaimed, as if he had seen a vision, “Don’t you see; they have been vaccinated!” Pasteur’s work ultimately saved many human lives.

Most of the important decisions in life involve incomplete information. Such decisions often involve so many complicated factors that a complete analysis is not practical or even possible. We are often forced into the position of making a guess based on limited information.

As the first quote reminds us, our chances of success are greatly improved if we have a “prepared mind.” The statistical methods you will learn in this book will help you achieve a prepared mind for the study of many different fields. The second quote reminds us that statistics is an important tool, but it is not a replacement for an in-depth knowledge of the field to which it is being applied.

The authors of this book want you to understand and enjoy statistics. The reading material will *tell you* about the subject. The examples will *show you* how it works. To understand, however, you must *get involved*. Guided exercises, calculator and computer applications, section and chapter problems, and writing exercises are all designed to get you involved in the subject. As you grow in your understanding of statistics, we believe you will enjoy learning a subject that has a world full of interesting applications.

Getting Started

PREVIEW QUESTIONS

- Why is statistics important? (SECTION 1.1)
- What is the nature of data? (SECTION 1.1)
- How can you draw a random sample? (SECTION 1.2)
- What are other sampling techniques? (SECTION 1.2)
- How can you design ways to collect data? (SECTION 1.3)
- Why are ethical considerations important? (SECTION 1.3)

FOCUS PROBLEMS

Where Have All the Fireflies Gone?

A feature article in *The Wall Street Journal* discusses the disappearance of fireflies. In the article, Professor Sara Lewis of Tufts University and other scholars express concern about the decline in the worldwide population of fireflies.

There are a number of possible explanations for the decline, including habitat reduction of woodlands, wetlands, and open fields; pesticides; and pollution. Artificial nighttime lighting might interfere with the Morse-code-like mating ritual of the fireflies. Some chemical companies pay a bounty for fireflies because the insects contain two rare chemicals used in medical research and electronic detection systems used in spacecraft.

What does any of this have to do with statistics?

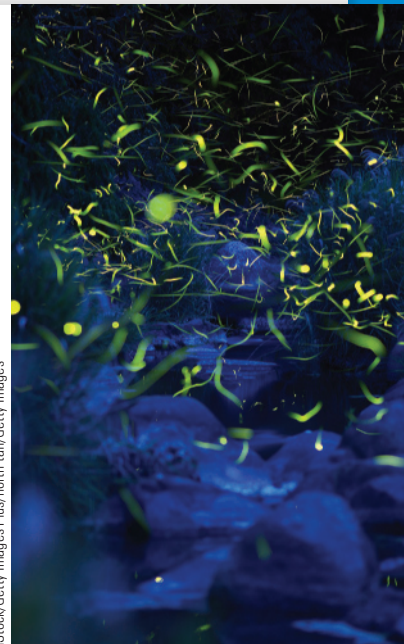
The truth, at this time, is that no one really knows (a) how much the world firefly population has declined or (b) how to explain the decline. The population of all fireflies is simply too large to study in its entirety.

In any study of fireflies, we must rely on incomplete information from samples. Furthermore, from these samples we must draw realistic conclusions that have statistical integrity. This is the kind of work that makes use of statistical methods to determine ways to collect, analyze, and investigate data.

Suppose you are conducting a study to compare firefly populations exposed to normal daylight/darkness conditions with firefly populations exposed to continuous light (24 hours a day). You set up two firefly colonies in a laboratory environment. The two colonies are identical except that one colony is exposed to normal daylight/darkness conditions and the other is exposed to continuous light. Each colony is populated with the same number of mature fireflies. After 72 hours, you count the number of living fireflies in each colony.

After completing this chapter, you will be able to answer the following questions:

- (a) Is this an experiment or an observation study? Explain.
- (b) Is there a control group? Is there a treatment group?



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Adapted from Ohio State University Firefly Files logo

For online student resources, visit the Brase/Brase, *Understanding Basic Statistics*, 8th edition web site at <http://www.cengage.com/statistics/brase>.

- (c) What is the variable in this study?
- (d) What is the level of measurement (nominal, interval, ordinal, or ratio) of the variable?

(See Problem 11 of the Chapter 1 Review Problems.)

SECTION 1.1

What Is Statistics?

FOCUS POINTS

- Identify variables in a statistical study.
- Distinguish between quantitative and qualitative variables.
- Identify populations and samples.
- Distinguish between parameters and statistics.
- Determine the level of measurement.
- Compare descriptive and inferential statistics.

Introduction

Decision making is an important aspect of our lives. We make decisions based on the information we have, our attitudes, and our values. Statistical methods help us examine information. Moreover, statistics can be used for making decisions when we are faced with uncertainties. For instance, if we wish to estimate the proportion of people who will have a severe reaction to a flu shot without giving the shot to everyone who wants it, statistics provides appropriate methods. Statistical methods enable us to look at information from a small collection of people or items and make inferences about a larger collection of people or items.

Procedures for analyzing data, together with rules of inference, are central topics in the study of statistics.

Statistics is the study of how to collect, organize, analyze, and interpret numerical information from data.

The subject of statistics is multifaceted. The following definition of statistics is found in the *International Encyclopedia of Statistical Science*, edited by Miodrag Lovric. Professor David Hand of Imperial College London—the president of the Royal Statistical Society—presents the definition in his article “Statistics: An Overview.”

Statistics is both the science of uncertainty and the technology of extracting information from data.

The statistical procedures you will learn in this book should supplement your built-in system of inference—that is, the results from statistical procedures and good sense should dovetail. Of course, statistical methods themselves have no power to work miracles. These methods can help us make some decisions, but not all conceivable decisions. Remember, even a properly applied statistical procedure is no more accurate than the data, or facts, on which it is based. Finally, statistical results should be interpreted by one who understands not only the methods, but also the subject matter to which they have been applied.

The general prerequisite for statistical decision making is the gathering of data. First, we need to identify the individuals or objects to be included in the study and the characteristics or features of the individuals that are of interest.

Individuals Variable

Individuals are the people or objects included in the study.
A **variable** is a characteristic of the individual to be measured or observed.

For instance, if we want to do a study about the people who have climbed Mt. Everest, then the individuals in the study are all people who have actually made it to the summit. One variable might be the height of such individuals. Other variables might be age, weight, gender, nationality, income, and so on. Regardless of the variables we use, we would not include measurements or observations from people who have not climbed the mountain.

The variables in a study may be *quantitative* or *qualitative* in nature.

Quantitative variable Qualitative variable

A **quantitative variable** has a value or numerical measurement for which operations such as addition or averaging make sense. A **qualitative variable** describes an individual by placing the individual into a category or group, such as male or female.

For the Mt. Everest climbers, variables such as height, weight, age, or income are *quantitative* variables. *Qualitative variables* involve nonnumerical observations such as gender or nationality. Sometimes qualitative variables are referred to as *categorical variables*.

Another important issue regarding data is their source. Do the data comprise information from *all* individuals of interest, or from just *some* of the individuals?

Categorical variable

Population data Sample data

In **population data**, the data are from *every* individual of interest.
In **sample data**, the data are from *only some* of the individuals of interest.

It is important to know whether the data are population data or sample data. Data from a specific population are fixed and complete. Data from a sample may vary from sample to sample and are *not* complete.

Population parameter

Sample statistic

A **population parameter** is a numerical measure that describes an aspect of a population.

A **sample statistic** is a numerical measure that describes an aspect of a sample.

For instance, if we have data from *all* the individuals who have climbed Mt. Everest, then we have population data. The proportion of males in the *population* of all climbers who have conquered Mt. Everest is an example of a *parameter*.

On the other hand, if our data come from just some of the climbers, we have sample data. The proportion of male climbers in the *sample* is an example of a *statistic*. Note that different samples may have different values for the proportion of male climbers. One of the important features of sample statistics is that they can vary from sample to sample, whereas population parameters are fixed for a given population.

LOOKING FORWARD

In later chapters we will use information based on a sample and sample statistics to estimate population parameters (Chapter 8) or make decisions about the value of population parameters (Chapters 9 and 10).

EXAMPLE 1

Using Basic Terminology

The Hawaii Department of Tropical Agriculture is conducting a study of ready-to-harvest pineapples in an experimental field.

- (a) The pineapples are the *objects* (individuals) of the study. If the researchers are interested in the individual weights of pineapples in the field, then the *variable* consists of weights. At this point, it is important to specify units of measurement



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and degrees of accuracy of measurement. The weights could be measured to the nearest ounce or gram. Weight is a *quantitative* variable because it is a numerical measure. If weights of *all* the ready-to-harvest pineapples in the field are included in the data, then we have a *population*. The average weight of all ready-to-harvest pineapples in the field is a *parameter*.

- (b) Suppose the researchers also want data on taste. A panel of tasters rates the pineapples according to the categories “poor,” “acceptable,” and “good.” Only some of the pineapples are included in the taste test. In this case, the *variable* is taste. This is a *qualitative* or *categorical* variable. Because only some of the pineapples in the field are included in the study, we have a *sample*. The proportion of pineapples in the sample with a taste rating of “good” is a *statistic*.

Throughout this text, you will encounter *guided exercises* embedded in the reading material. These exercises are included to give you an opportunity to work immediately with new ideas. The questions guide you through appropriate analysis. Cover the answers on the right side (an index card will fit this purpose). After you have thought about or written down *your own response*, check the answers. If there are several parts to an exercise, check each part before you continue. You should be able to answer most of these exercise questions, but don’t skip them—they are important.

GUIDED EXERCISE 1

Using Basic Terminology

How important is music education in school (K–12)? *The Harris Poll* did an online survey of 2286 adults (aged 18 and older) within the United States. Among the many questions, the survey asked if the respondents agreed or disagreed with the statement “Learning and habits from music education equip people to be better team players in their careers.” In the most recent survey, 71% of the study participants agreed with the statement.

- | | |
|---|---|
| (a) Identify the individuals of the study and the variable. | ➔ The individuals are the 2286 adults who participated in the online survey. The variable is the response agree or disagree with the statement that music education equips people to be better team players in their careers. |
| (b) Do the data comprise a sample? If so, what is the underlying population? | ➔ The data comprise a sample of the population of responses from all adults in the United States. |
| (c) Is the variable qualitative or quantitative? | ➔ Qualitative—the categories are the two possible responses: agrees or disagrees with the statement that music education equips people to be better team players in their careers. |
| (d) Identify a quantitative variable that might be of interest. | ➔ Age or income might be of interest. |
| (e) Is the proportion of respondents in the sample who agree with the statement regarding music education and effect on careers a statistic or a parameter? | ➔ Statistic—the proportion is computed from sample data. |

Levels of Measurement: Nominal, Ordinal, Interval, Ratio

We have categorized data as either qualitative or quantitative. Another way to classify data is according to one of the four *levels of measurement*. These levels indicate the type of arithmetic that is appropriate for the data, such as ordering, taking differences, or taking ratios.

Levels of Measurement

Nominal level

Ordinal level

Interval level

Ratio level

LEVELS OF MEASUREMENT

The **nominal level of measurement** applies to data that consist of names, labels, or categories. There are no implied criteria by which the data can be ordered from smallest to largest.

The **ordinal level of measurement** applies to data that can be arranged in order. However, differences between data values either cannot be determined or are meaningless.

The **interval level of measurement** applies to data that can be arranged in order. In addition, differences between data values are meaningful.

The **ratio level of measurement** applies to data that can be arranged in order. In addition, both differences between data values and ratios of data values are meaningful. Data at the ratio level have a true zero.

EXAMPLE 2

Levels of Measurement

Identify the type of data.

- (a) Taos, Acoma, Zuni, and Cochiti are the names of four Native American pueblos from the population of names of all Native American pueblos in Arizona and New Mexico.

SOLUTION: These data are at the *nominal* level. Notice that these data values are simply names. By looking at the name alone, we cannot determine if one name is “greater than or less than” another. Any ordering of the names would be numerically meaningless.

- (b) In a high school graduating class of 319 students, Jim ranked 25th, June ranked 19th, Walter ranked 10th, and Julia ranked 4th, where 1 is the highest rank.

SOLUTION: These data are at the *ordinal* level. Ordering the data clearly makes sense. Walter ranked higher than June. Jim had the lowest rank, and Julia the highest. However, numerical differences in ranks do not have meaning. The difference between June’s and Jim’s ranks is 6, and this is the same difference that exists between Walter’s and Julia’s ranks. However, this difference doesn’t really mean anything significant. For instance, if you looked at grade point average, Walter and Julia may have had a large gap between their grade point averages, whereas June and Jim may have had closer grade point averages. In any ranking system, it is only the relative standing that matters. Computed differences between ranks are meaningless.

- (c) Body temperatures (in degrees Celsius) of trout in the Yellowstone River.

SOLUTION: These data are at the *interval* level. We can certainly order the data, and we can compute meaningful differences. However, for Celsius-scale temperatures, there is not an inherent starting point. The value 0°C may seem to be a starting point, but this value does not indicate the state of “no heat.” Furthermore, it is not correct to say that 20°C is twice as hot as 10°C .

- (d) Length of trout swimming in the Yellowstone River.

SOLUTION: These data are at the *ratio* level. A 45-cm trout is three times as long as a 15-cm trout. Observe that we can divide 15 into 45 to determine a meaningful *ratio* of trout lengths.



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In summary, there are four levels of measurement. The nominal level is considered the lowest, and in ascending order we have the ordinal, interval, and ratio levels. In general, calculations based on a particular level of measurement may not be appropriate for a lower level.

PROCEDURE

How to determine the level of measurement

The levels of measurement, listed from lowest to highest, are nominal, ordinal, interval, and ratio. To determine the level of measurement of data, state the *highest level* that can be justified for the entire collection of data. Consider which calculations are suitable for the data.

Level of Measurement	Suitable Calculation
Nominal	We can put the data into categories.
Ordinal	We can order the data from smallest to largest or “worst” to “best.” Each data value can be <i>compared</i> with another data value.
Interval	We can order the data and also take the differences between data values. At this level, it makes sense to compare the differences between data values. For instance, we can say that one data value is 5 more than or 12 less than another data value.
Ratio	We can order the data, take differences, and also find the ratio between data values. For instance, it makes sense to say that one data value is twice as large as another.



What Does the Level of Measurement Tell Us?

The level of measurement tells us which arithmetic processes are appropriate for the data. This is important because different statistical processes require various kinds of arithmetic. In some instances all we need to do is count the number of data that meet specified criteria. In such cases nominal (and higher) data levels are all appropriate. In other cases we need to order the data, so nominal data would not be suitable. Many other statistical processes require division, so data need to be at the ratio level. Just keep the nature of the data in mind before beginning statistical computations.

GUIDED EXERCISE 2

Levels of Measurement

The following describe different data associated with a state senator. For each data entry, indicate the corresponding *level of measurement*.

- (a) The senator’s name is Sam Wilson.  Nominal level
- (b) The senator is 58 years old.  Ratio level. Notice that age has a meaningful zero. It makes sense to give age ratios. For instance, Sam is twice as old as someone who is 29.

Continued

Guided Exercise 2 *continued*

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| (c) The years in which the senator was elected to the Senate are 2000, 2006, and 2012. | ➔ | Interval level. Dates can be ordered, and the difference between dates has meaning. For instance, 2006 is 6 years later than 2000. However, ratios do not make sense. The year 2000 is not twice as large as the year 1000. In addition, the year 0 does not mean “no time.” |
| (d) The senator’s total taxable income last year was \$878,314. | ➔ | Ratio level. It makes sense to say that the senator’s income is 10 times that of someone earning \$87,831. |
| (e) The senator surveyed his constituents regarding his proposed water protection bill. The choices for response were strongly support, support, neutral, against, or strongly against. | ➔ | Ordinal level. The choices can be ordered, but there is no meaningful numerical difference between two choices. |
| (f) The senator’s marital status is “married.” | ➔ | Nominal level |
| (g) A leading news magazine claims that the senator is ranked seventh for his voting record on bills regarding public education. | ➔ | Ordinal level. Ranks can be ordered, but differences between ranks may vary in meaning. |

CRITICAL THINKING

“Data! Data! Data!” he cried impatiently. “I can’t make bricks without clay.” Sherlock Holmes said these words in *The Adventure of the Copper Beeches* by Sir Arthur Conan Doyle.

Reliable statistical conclusions require reliable data. This section has provided some of the vocabulary used in discussing data. As you read a statistical study or conduct one, pay attention to the nature of the data and the ways they were collected.

When you select a variable to measure, be sure to specify the process and requirements for measurement. For example, if the variable is the weight of ready-to-harvest pineapples, specify the unit of weight, the accuracy of measurement, and maybe even the particular scale to be used. If some weights are in ounces and others in grams, the data are fairly useless.

Another concern is whether or not your measurement instrument truly measures the variable. Just asking people if they know the geographic location of the island nation of Fiji may not provide accurate results. The answers may reflect the fact that the respondents want you to think they are knowledgeable. Asking people to locate Fiji on a map may give more reliable results.

The level of measurement is also an issue. You can put numbers into a calculator or computer and do all kinds of arithmetic. However, you need to judge whether the operations are meaningful. For ordinal data such as restaurant rankings, you can’t conclude that a 4-star restaurant is “twice as good” as a 2-star restaurant, even though the number 4 is twice 2.

Continued